



# Flamingo: Multi-Round Single-Server Secure Aggregation with Applications to Private Federated Learning

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# Data-driven applications nowadays

Service providers collect and analyze user data in order to provide customized functionalities.



# Data-driven applications nowadays

Simply put, to protect users at scale, we rely on machine learning powered by user feedback to catch spam and help us identify patterns in large data sets—making it easier to adapt quickly to ever-changing spam tactics. Gmail employs a number of AI-driven filters that determine what gets marked as spam. These filters look at a variety of signals, including characteristics of the IP address, domains/subdomains, whether bulk senders are authenticated, and user input. User feedback, such as when a user marks a certain email as spam or signals they want a sender's emails in their inbox, is key to this filtering process, and our filters learn from user actions.



Art

Creating a text classifier model

Amazon

Train a machine learning model to classify natural language text.

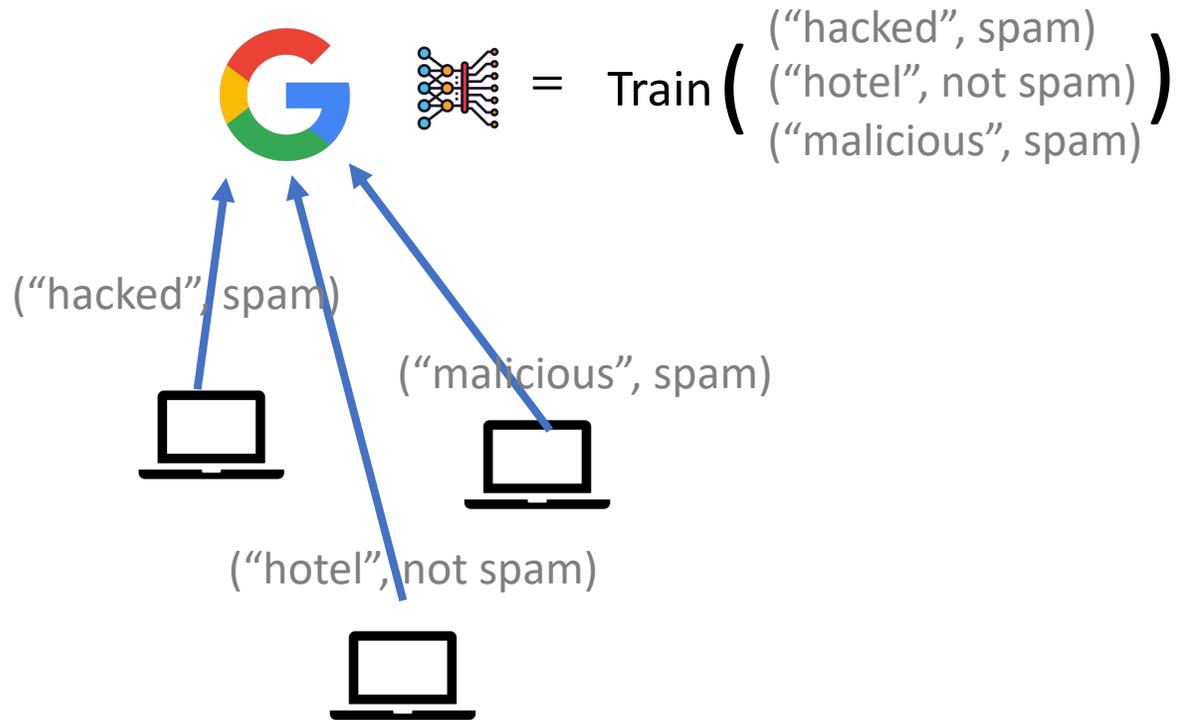
Elevate the customer experience with ML-powered personalization

Get started with Amazon Personalize



# Centralized vs. decentralized training

## Centralized



## Decentralized

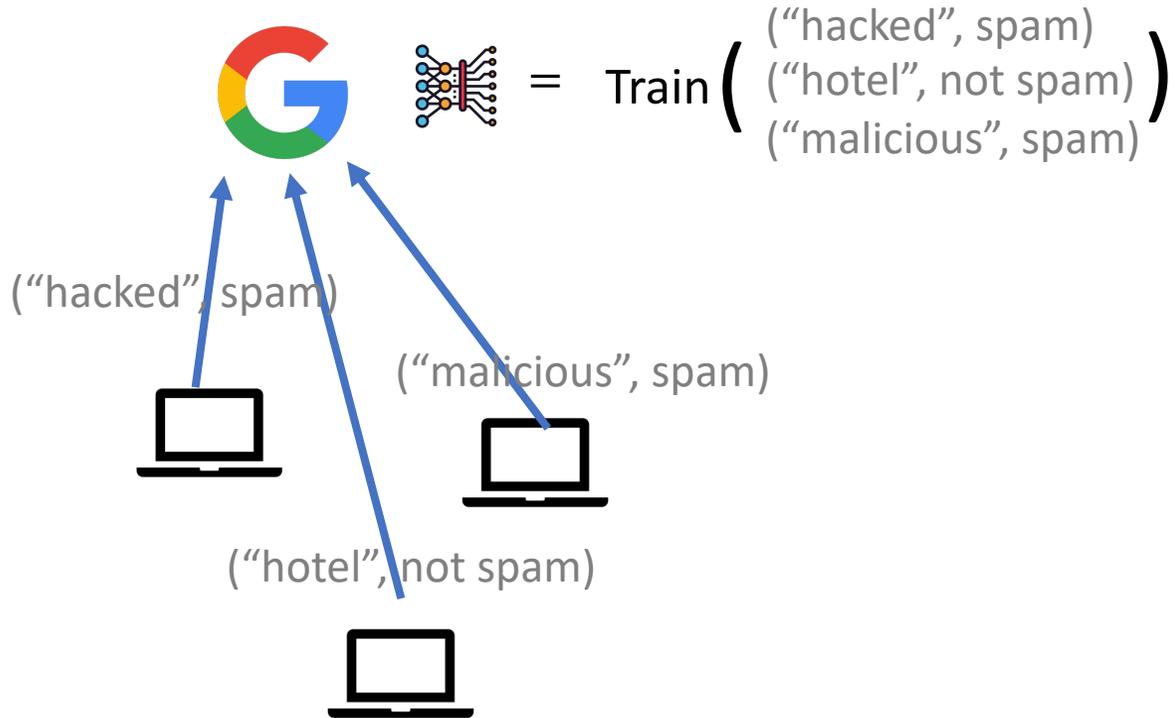
“Federated learning” [McMahan et al. in 2016]

Many clients (users) collaboratively train a model under the orchestration of a central server (service provider).

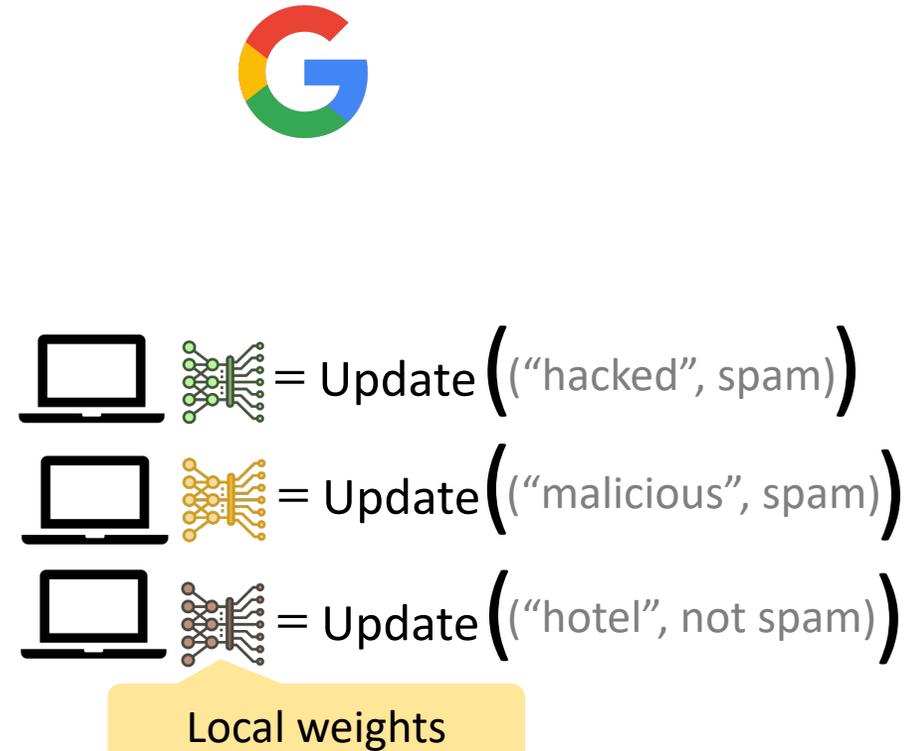
Data never leaves user devices!

# Centralized vs. decentralized training

## Centralized

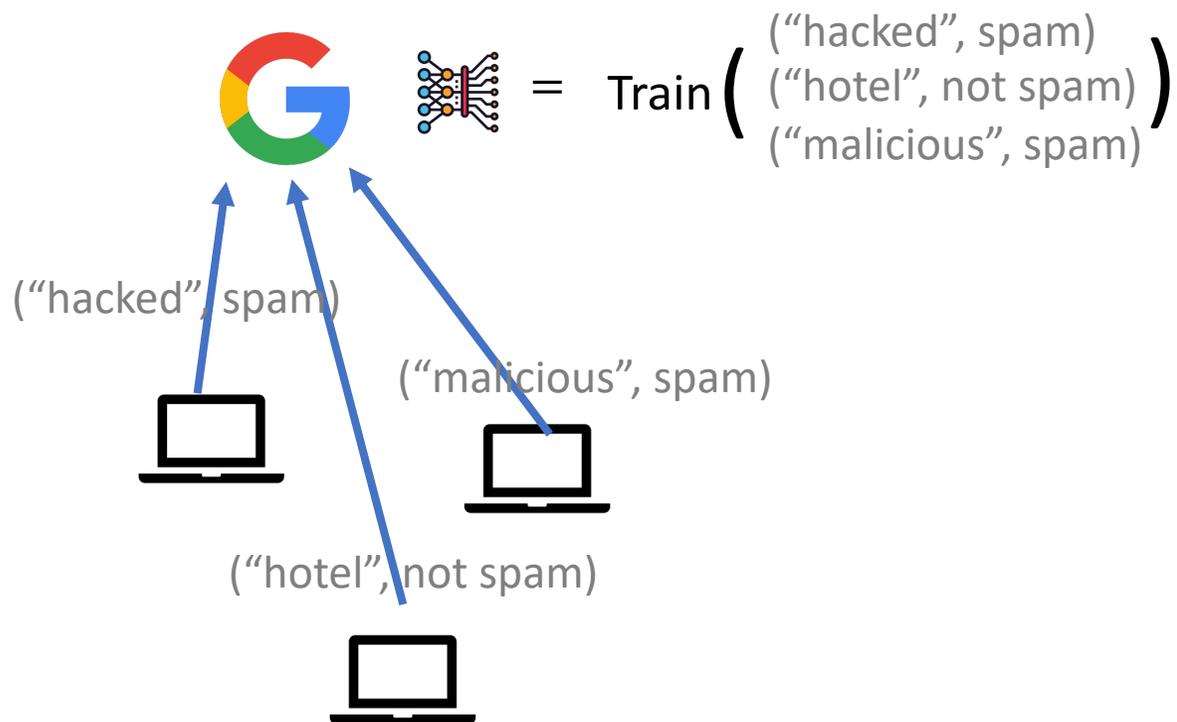


## Decentralized

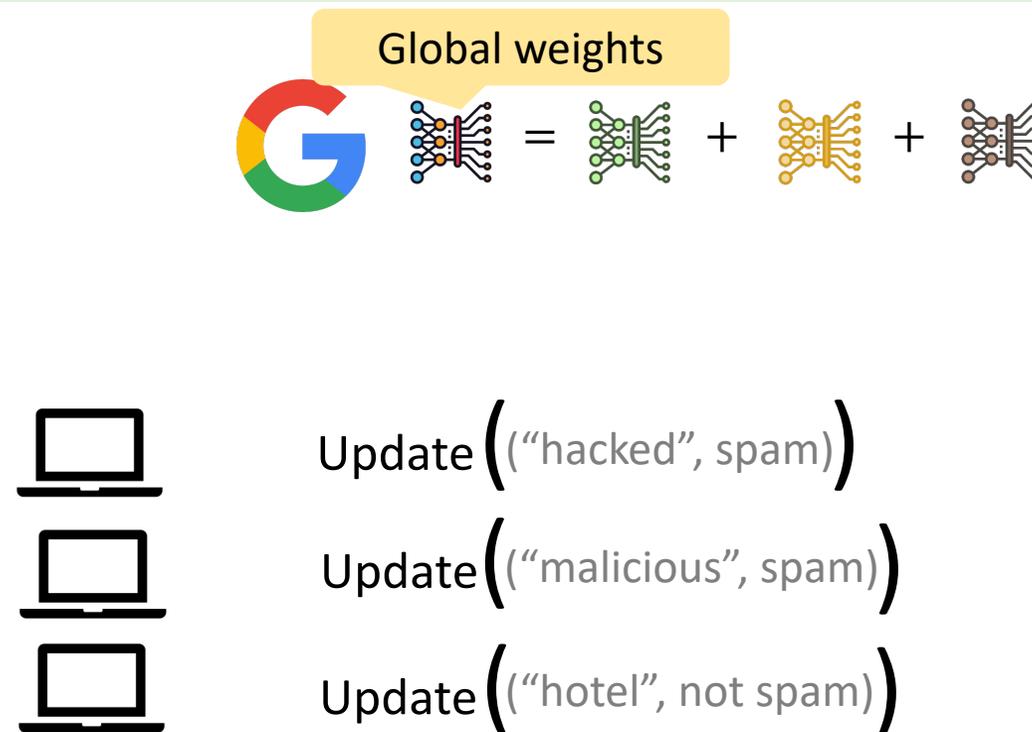


# Centralized vs. decentralized training

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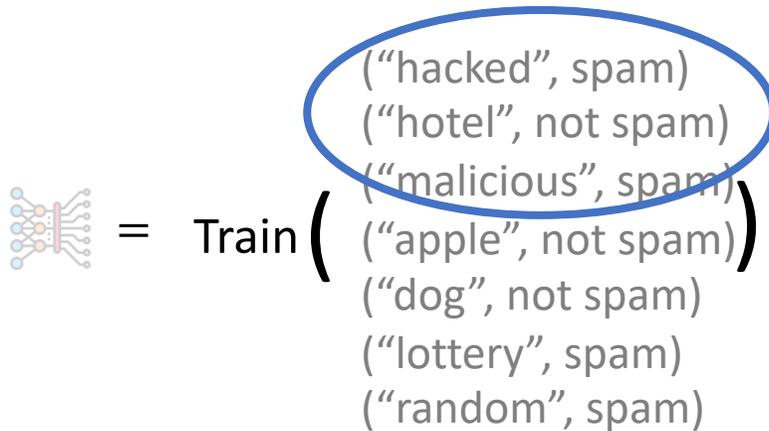


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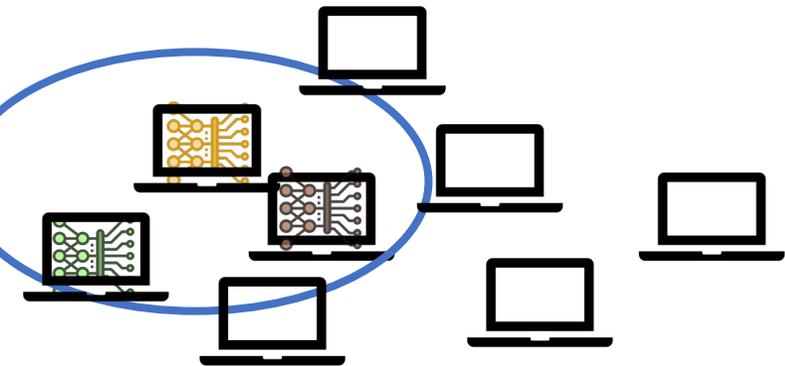


# Centralized vs. decentralized training

## Centralized



A few hundreds to a few thousands of clients

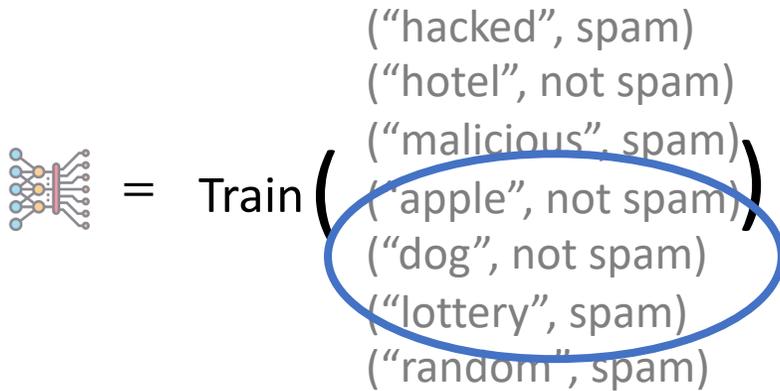


## Decentralized

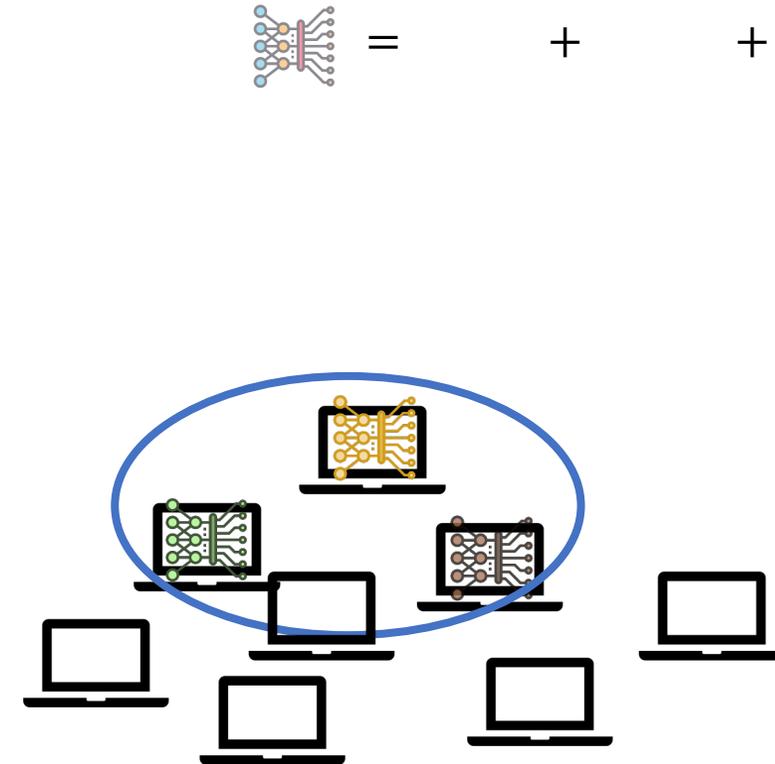


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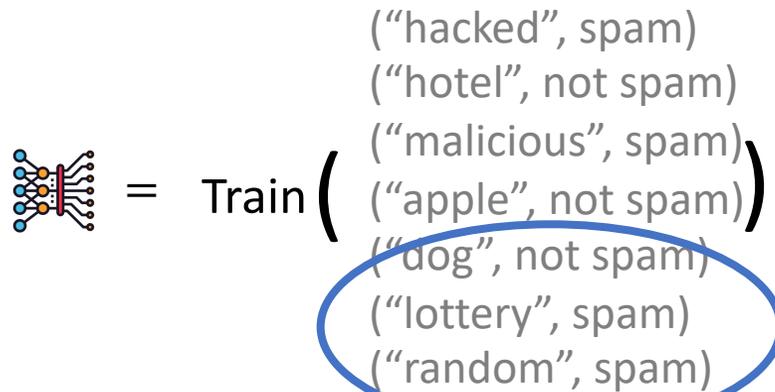


## Decentralized

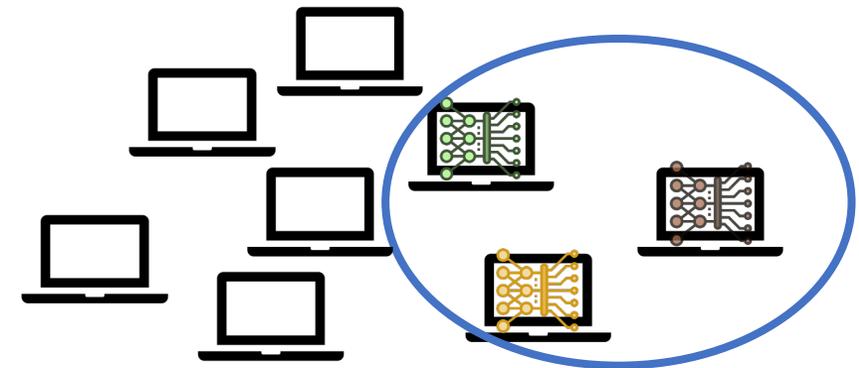


# Centralized vs. decentralized training

## Centralized



## Decentralized



# Federated learning: steps forward

- Weights do not necessarily hide data: [inference attack](#)  
[Zhu et al. 2019]



("hacked", spam)

- Training does not need individual weights; only the sum is needed

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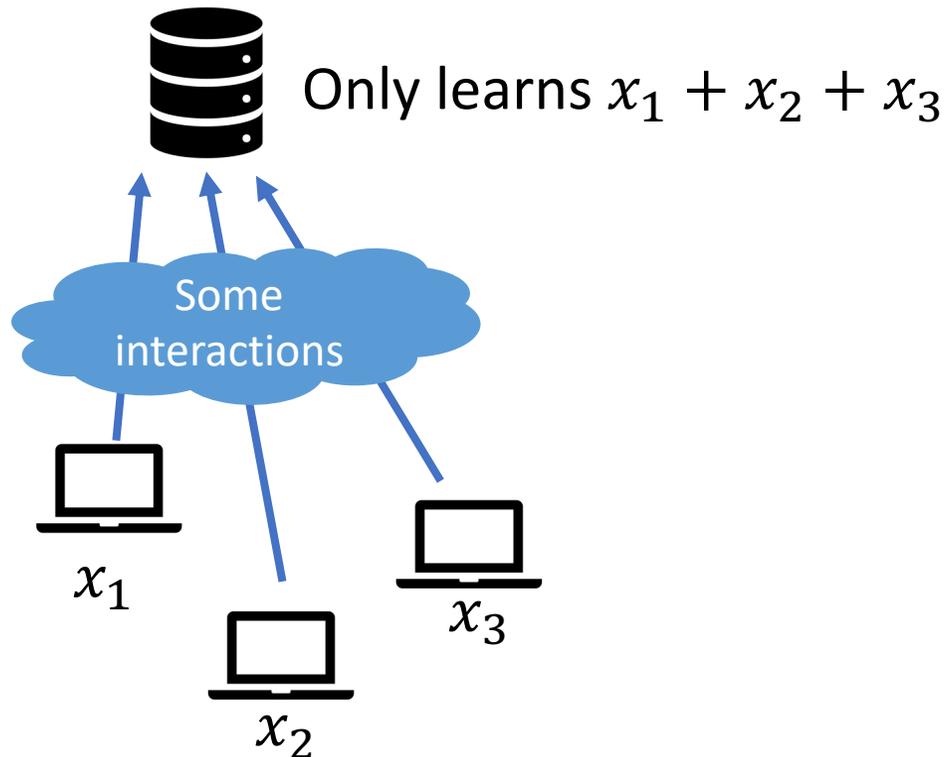


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# Secure aggregation for federated learning

- Secure aggregation (A special case of MPC [Yao 1986])

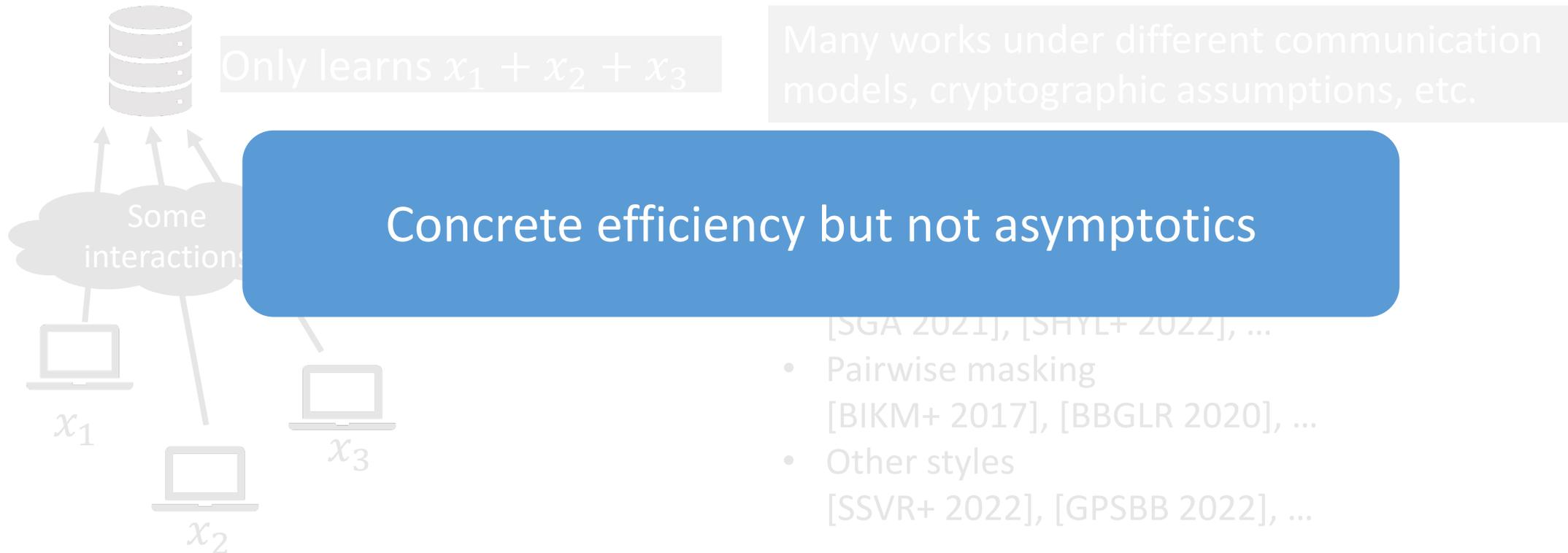


Many works under different communication models, cryptographic assumptions, etc.

- Secret sharing  
[KRKR 2020], [DSQG+ 2022], ...
- Threshold homomorphic encryption  
[SGA 2021], [SHYL+ 2022], ...
- Pairwise masking  
[BIKM+ 2017], [BBGLR 2020], ...
- Other styles  
[SSVR+ 2022], [GPSBB 2022], ...

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# Federated learning has complex setting

- From the federation side—restricted clients (mobile devices)
  - Limited computation power
  - Unstable network connection
- From the machine learning side—large parameters
  - Inputs: model weights, e.g., ~500K in popular models for CIFAR100
  - Participants: 100-5000 per iteration
  - Training: many iterations, e.g., ~300 for CIFAR100

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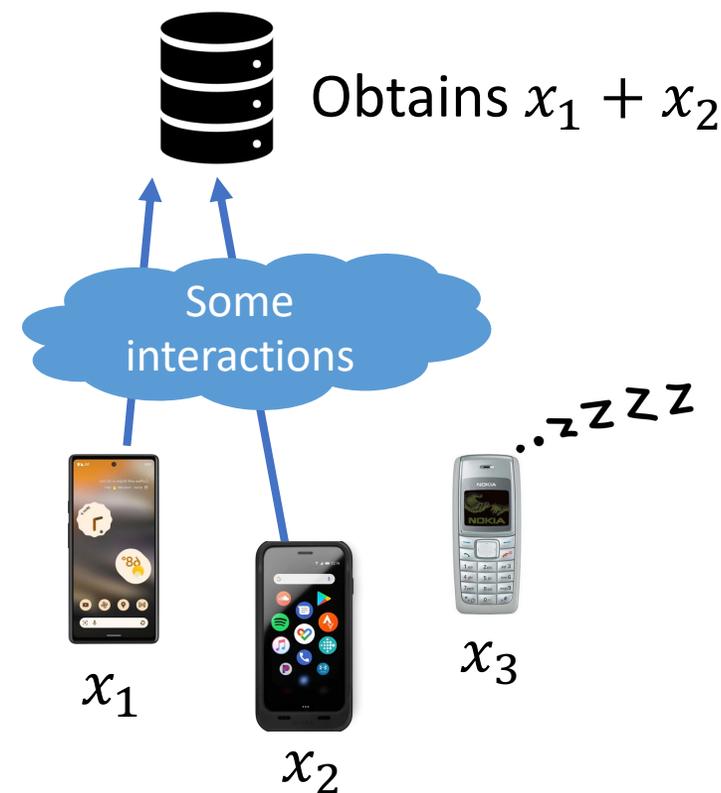
# Prior designs are not the best fit for a full training

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One summation: multiple round trips, some of which are expensive

# Having fewer round trips is important

- Reduce bias and improve quality
- Reduce run time  
Will discuss in evaluation section  
why round trips matter a lot



# We propose Flamingo

- From the federation side—restricted clients (mobile devices)

- Limited computation power
- Unstable network connection

Lightweight client computation

Tolerate dropouts at any point

- From the machine learning side—large parameters

- Inputs: model weights, e.g., ~500K in popular models for
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Can practically run for a full training session

Same threat model as in prior work: a malicious adversary controlling the server and a subset of the clients

# Flamingo has two key ideas

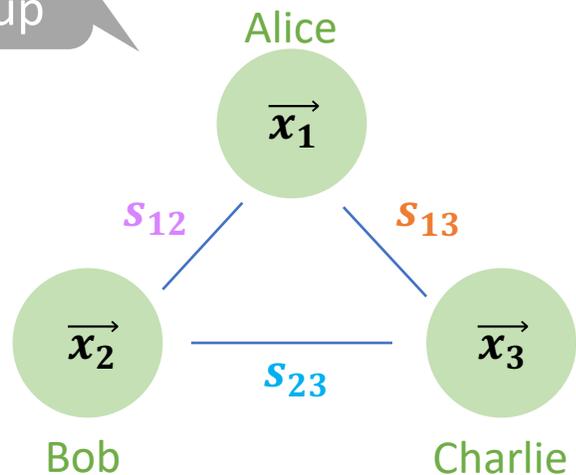
- A fault-tolerant private sum protocol based on pairwise secrets and threshold decryption
- A way to reuse pairwise secrets over many iterations

# A fault-tolerant private sum protocol

## Pairwise secrets

BIKM+ 2017,  
BBGLR 2020

Take some cost  
to set them up



$$\vec{v}_1 = \vec{x}_1 + \text{PRG}(s_{12}) + \text{PRG}(s_{13})$$

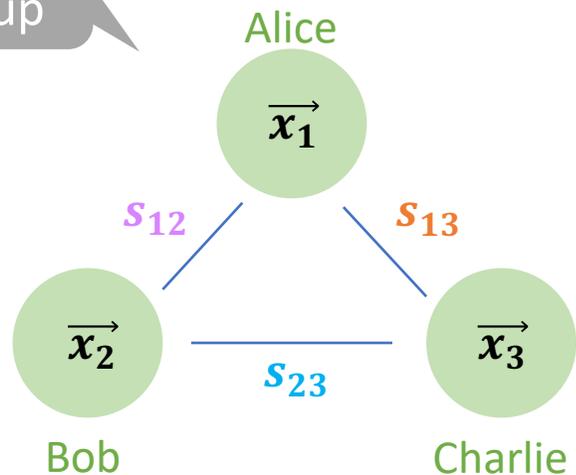
# A fault-tolerant private sum protocol

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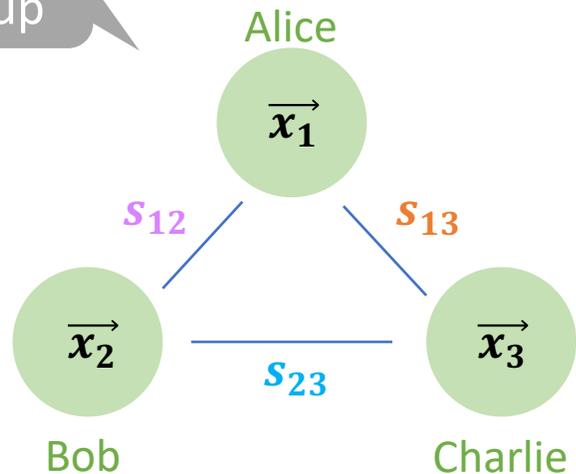
$$\begin{aligned}\vec{v}_1 &= \vec{x}_1 + \cancel{\text{PRG}(s_{12})} + \cancel{\text{PRG}(s_{13})} \\ \vec{v}_2 &= \vec{x}_2 - \cancel{\text{PRG}(s_{12})} + \cancel{\text{PRG}(s_{23})} \\ \vec{v}_3 &= \vec{x}_3 - \cancel{\text{PRG}(s_{13})} - \cancel{\text{PRG}(s_{23})}\end{aligned}$$

# A fault-tolerant private sum protocol

## Pairwise secrets

BIKM+ 2017,  
BBGLR 2020

Take some cost  
to set them up





$$\sum_{i=1}^3 \vec{v}_i = \sum_{i=1}^3 \vec{x}_i$$

$$\vec{v}_1 = \vec{x}_1 + \cancel{\text{PRG}(s_{12})} + \cancel{\text{PRG}(s_{13})}$$

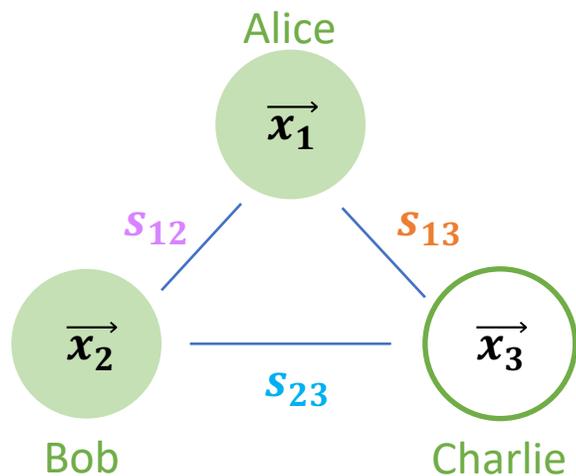
$$\vec{v}_2 = \vec{x}_2 - \cancel{\text{PRG}(s_{12})} + \cancel{\text{PRG}(s_{23})}$$

$$\vec{v}_3 = \vec{x}_3 - \cancel{\text{PRG}(s_{13})} - \cancel{\text{PRG}(s_{23})}$$

Efficient despite large inputs

# A fault-tolerant private sum protocol

## Pairwise secrets



Went offline...

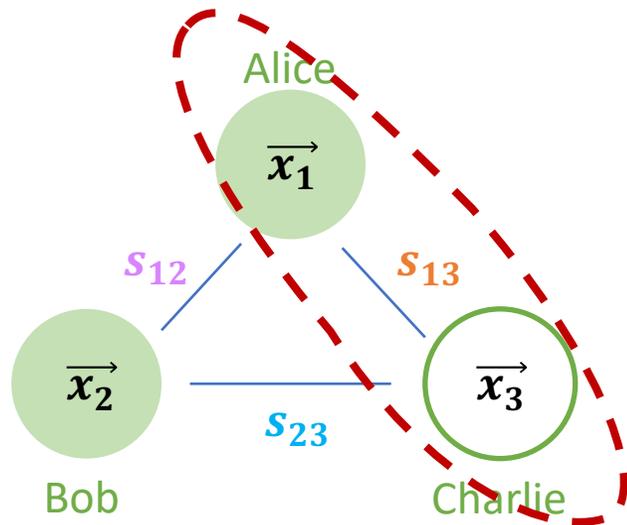
$$\vec{v}_1 = \vec{x}_1 + \cancel{\text{PRG}(s_{12})} + \text{PRG}(s_{13})$$

$$\vec{v}_2 = \vec{x}_2 - \cancel{\text{PRG}(s_{12})} + \text{PRG}(s_{23})$$

Reveal the secrets  
to the server!

# A fault-tolerant private sum protocol

## Threshold decryption

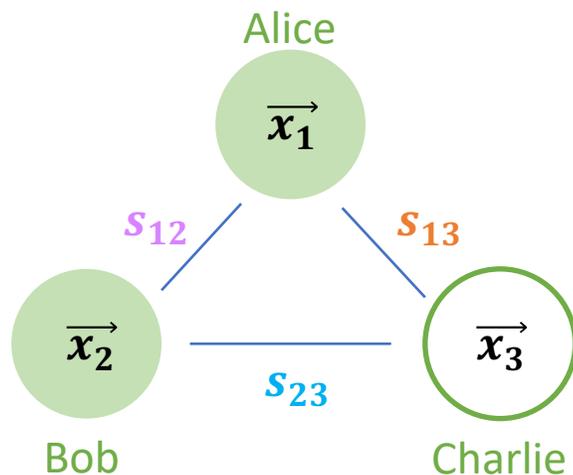


$$\vec{v}_1 = \vec{x}_1 + \text{PRG}(s_{12}) + \text{PRG}(s_{13})$$

Diagram illustrating the threshold decryption process. A vertical bar represents the vector  $\vec{v}_1$ , which is equal to the sum of the input vector  $\vec{x}_1$  and two pseudorandom generators (PRG) applied to the shared keys  $s_{12}$  and  $s_{13}$ . The PRG outputs are shown as grey bars, and the input vector  $\vec{x}_1$  is shown as a green bar. The PRG outputs are encrypted using a public key (PK) and are shown as grey bars at the bottom, with a red dashed oval around the  $\text{Enc}(PK, s_{13})$  component.

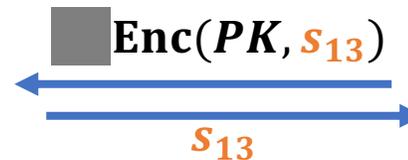
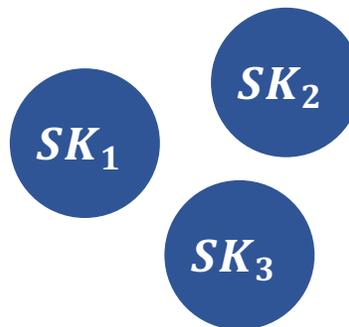
# A fault-tolerant private sum protocol

## Threshold decryption



Recovery is lightweight

Decryptors



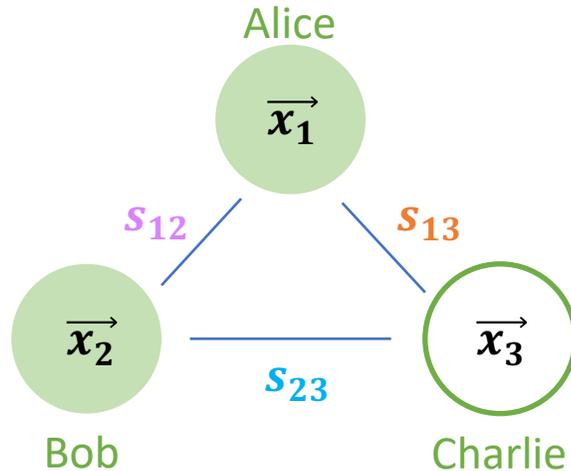
A random (small) subset of clients

# A fault-tolerant private sum protocol

## Threshold decryption



$\vec{v}_1$   $\vec{v}_2$   $s_{13}$   $s_{23}$

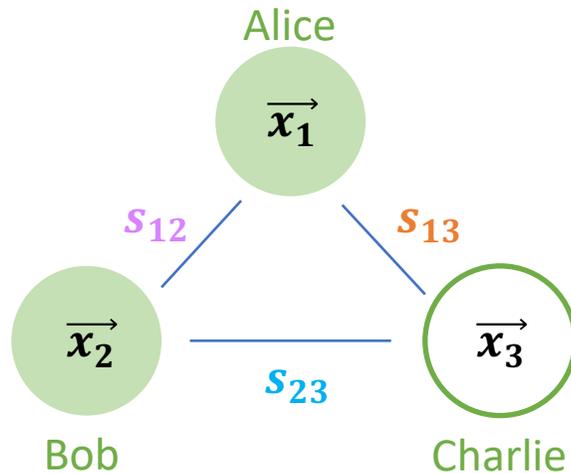


$$\vec{v}_1 = \vec{x}_1 + \text{PRG}(s_{12}) + \text{PRG}(s_{13})$$

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# A fault-tolerant private sum protocol

## Threshold decryption



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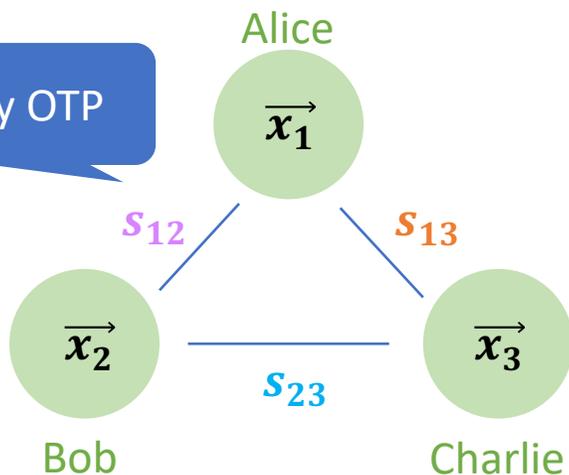
$$\vec{v}_2 = \vec{x}_2 - \text{PRG}(s_{12}) + \text{PRG}(s_{23}) - \text{PRG}(s_{13}) - \text{PRG}(s_{23})$$

$$\vec{v}_1 + \vec{v}_2 - \text{PRG}(s_{13}) - \text{PRG}(s_{23}) = \vec{x}_1 + \vec{x}_2$$

# Reusing the secrets

Simple idea, but cannot work for [BBGLR 2020] due to a crucial design difference for fault tolerance

Essentially OTP



Iteration  $t$ :  $s_{12}^t = \text{PRF}(s_{12}, t)$

$$\vec{v}_1 = \vec{x}_1 + \text{PRG}(s_{12}^t) + \text{PRG}(s_{13}^t)$$

$\text{Enc}(PK, s_{12}^t)$   
  $\text{Enc}(PK, s_{13}^t)$

With the two key ideas →

Do the costly setup once,  
and run the lightweight sum many times

# More details in the paper

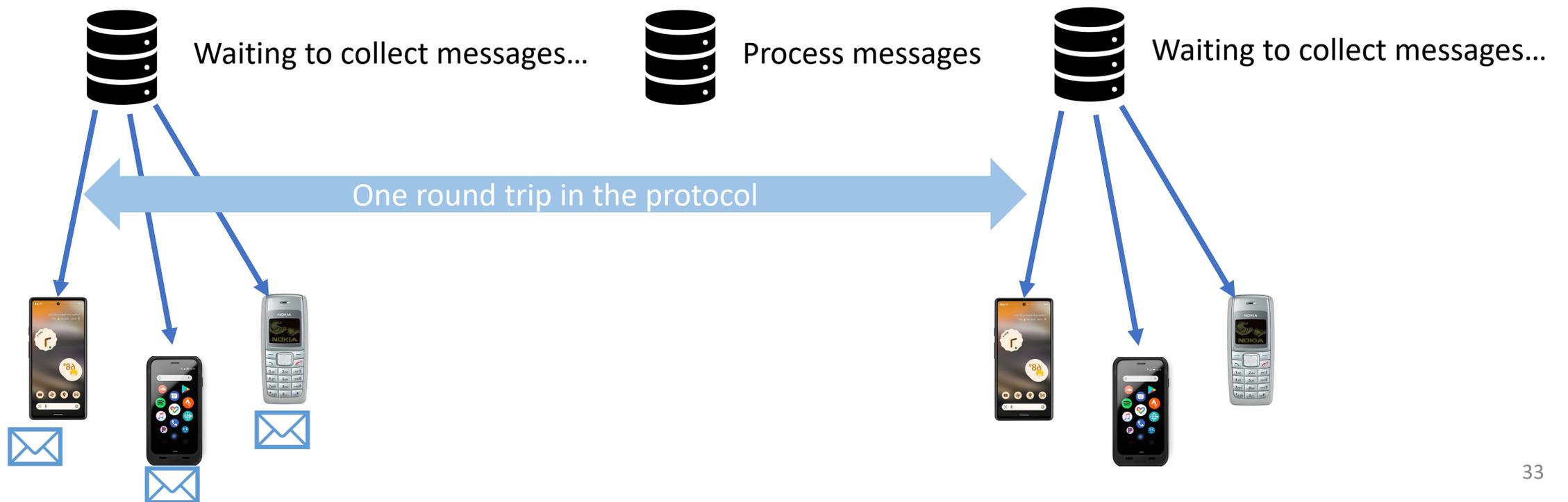
- How **decryptors** work
  - Selection
  - Sharing of  $SK$
  - Switching decryptors over time
- How **setup** is done
- How to achieve **malicious security**
- Efficient instantiation of cryptographic primitives, system-level optimizations

# Evaluation results

- What is the right factor to look at?
  - Computation cost was the focus: [BIKM+ 2017] → [BBGLR 2020]
  - When computation is made cheap, what matters is the “waiting time”

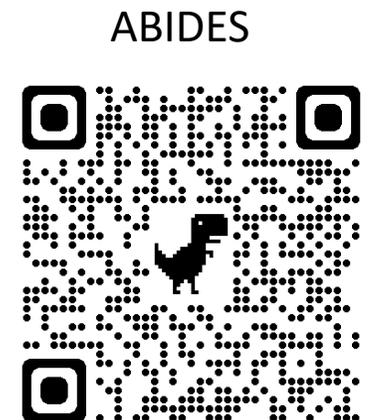
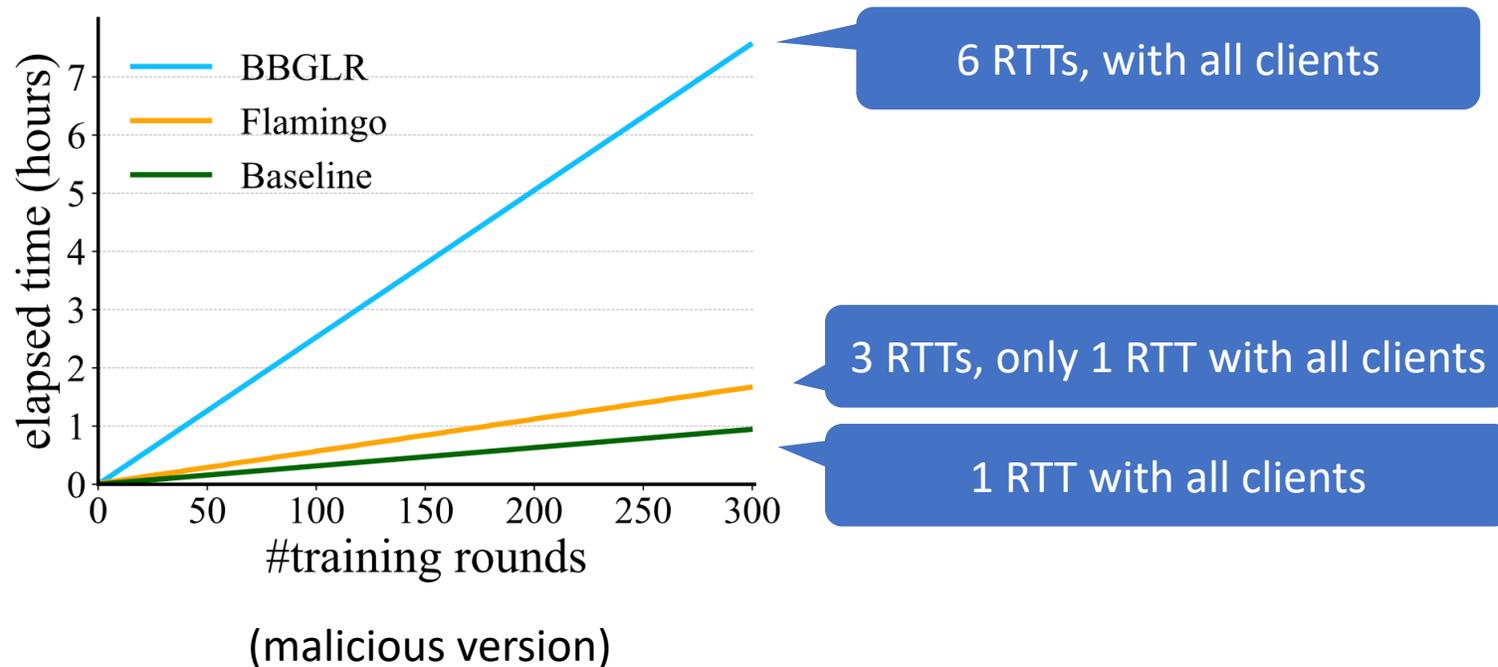
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# Evaluation results

- Feasibility of training a neural network on CIFAR100
- Simulation using a multi-agent messaging system ABIDES

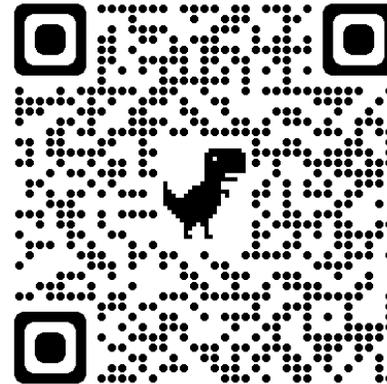


# Summary

- This work: A secure aggregation system that handles real-world federated training tasks
- Many interesting future directions
  - Validation of client inputs
  - Stronger security, e.g., adaptive adversary



paper



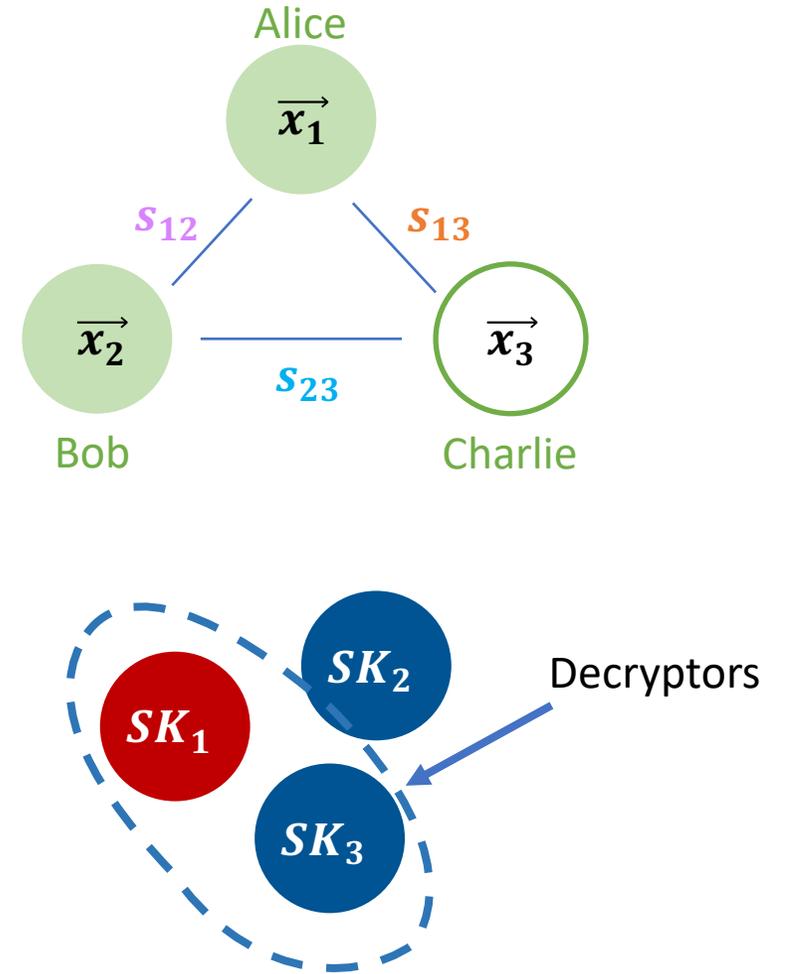
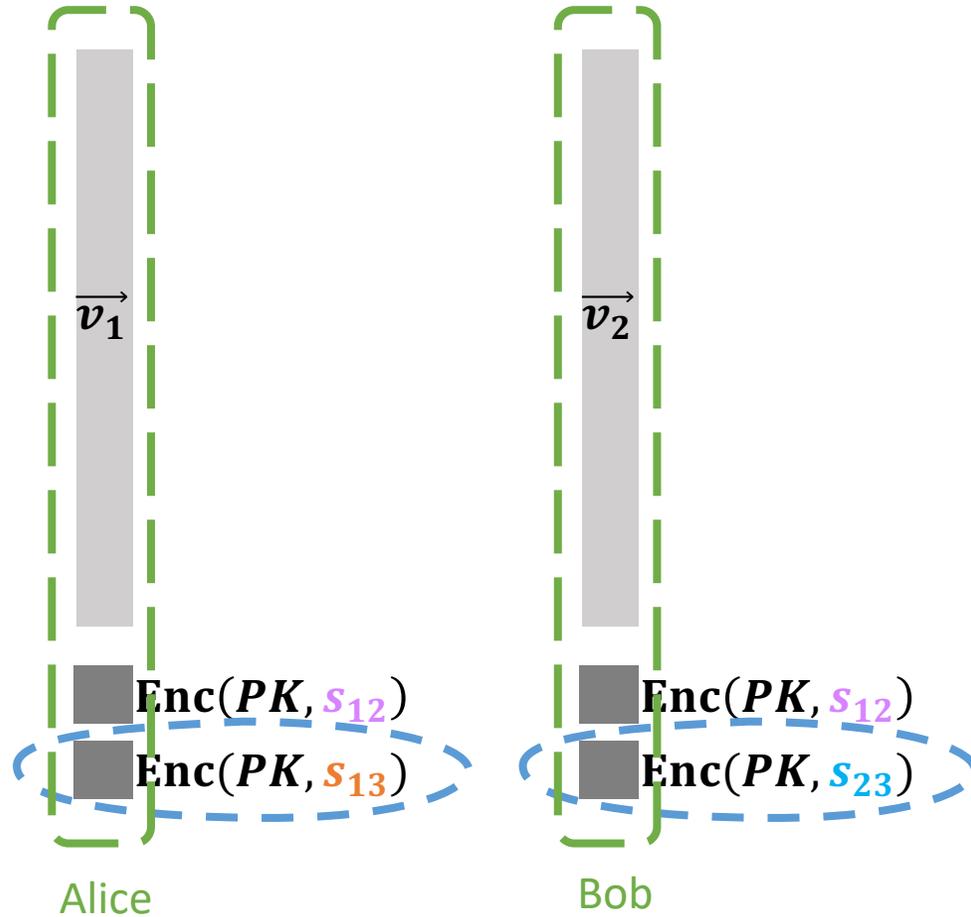
code



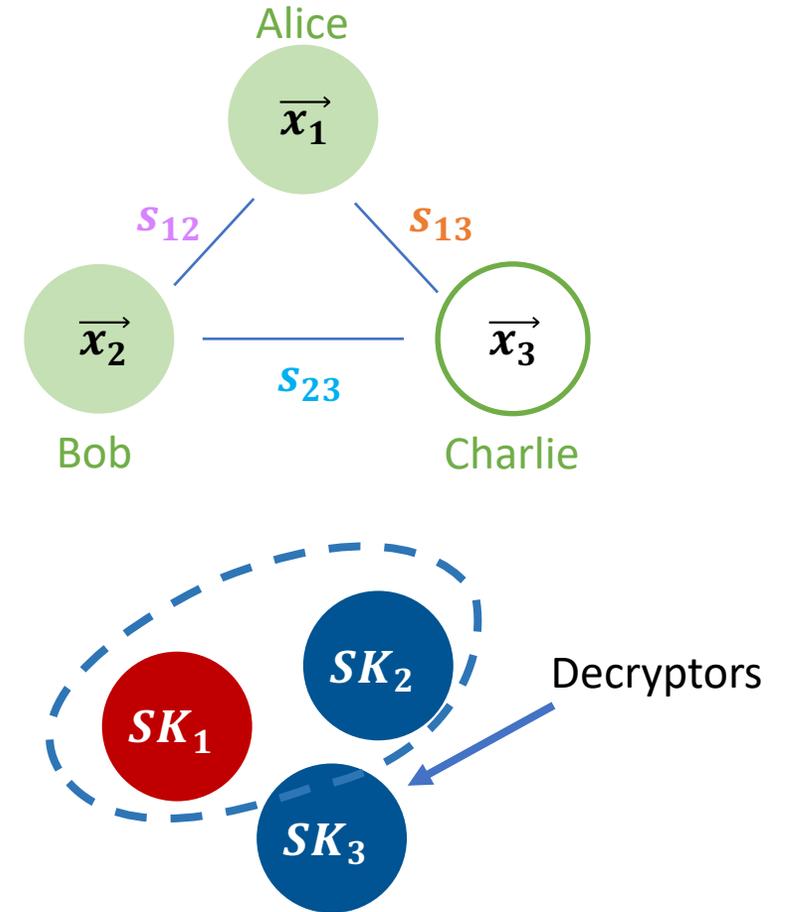
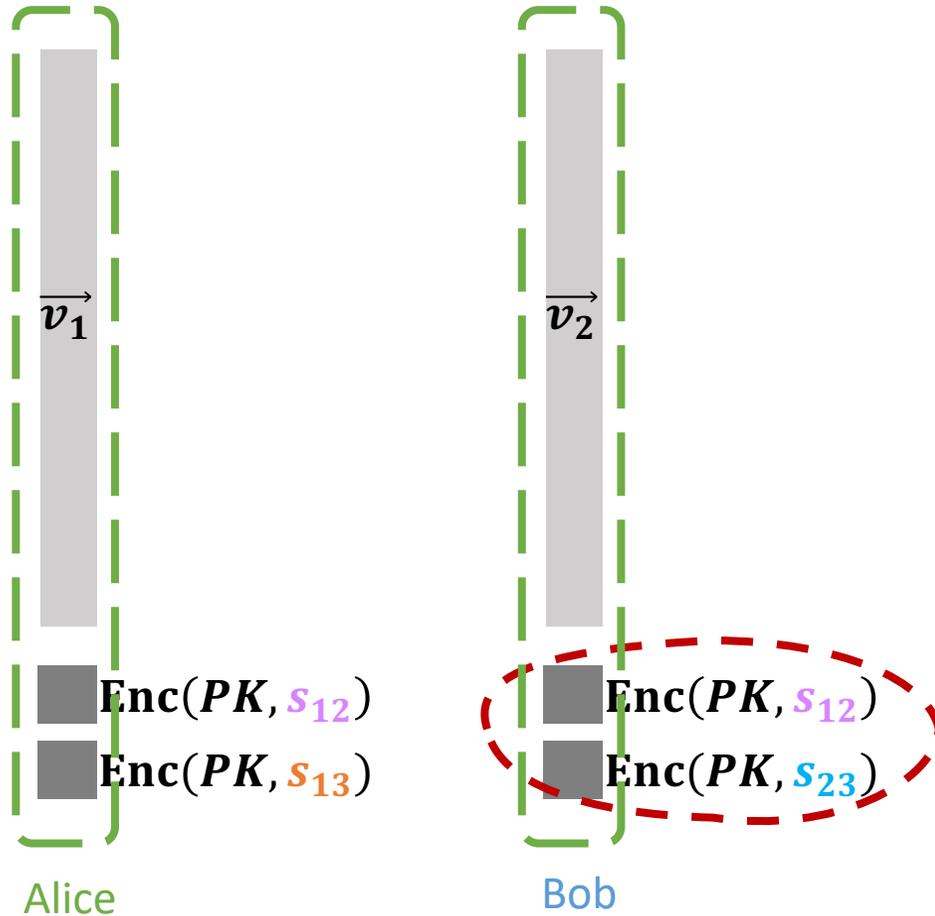
Thanks!

# Backup Slides

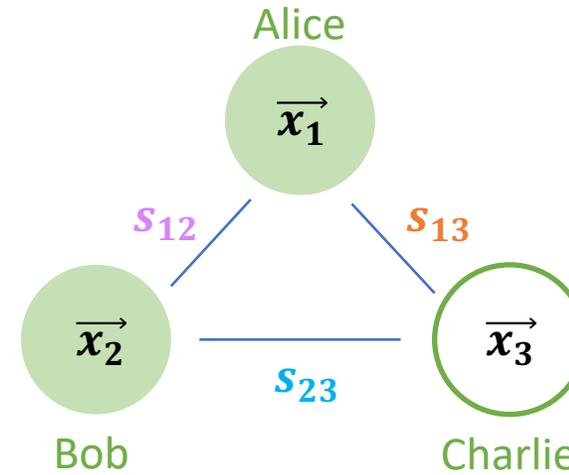
# Malicious security



# Malicious security

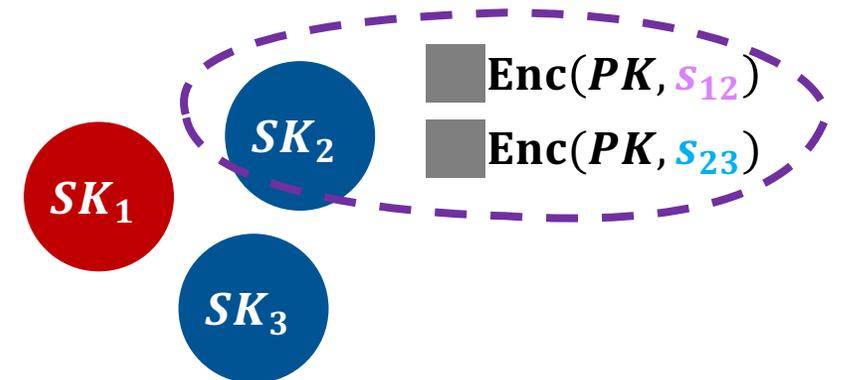
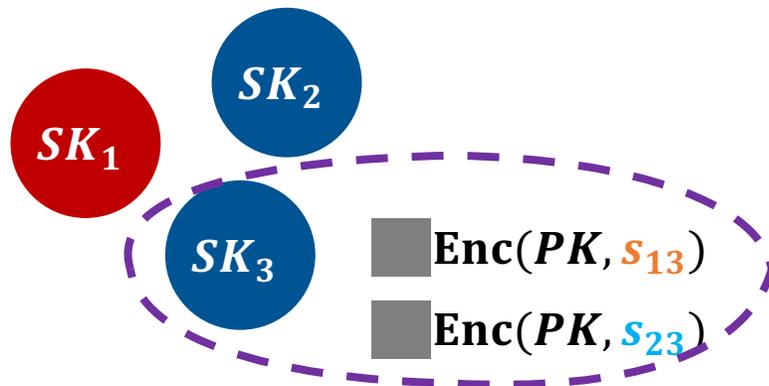


# A cross-check round



Key idea:

Honest decryptors agree on what to decrypt



# A fault-tolerant sum with malicious security

